



Section 1. Electrical engineering

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THERMAL AND ENERGY CHARACTERISTICS OF A COGENERATIVE FRACTAL SOLAR COLLECTOR

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Abstract

The paper considers the design and thermal energy characteristics of a new type of fractal solar collector operating in cogeneration mode. The principle of operation of the proposed solar installation is given. The efficiency of using solar insolation in comparison with flat solar collectors is shown.

Keywords: *Fractal, solar collector, cogeneration mode, solar insolation, electric energy*

Introduction

A solar collector is a device for collecting thermal energy from the Sun (solar installation), carried by visible light and near infrared radiation. Unlike solar panels, which produce electricity directly, the solar collector heats the coolant material.

As is known, thermal energy analysis is especially important for solar installations, since this natural source is characterized by stochasticity and strong energy dissipation in space, which requires a design change to increase the use of solar energy. The problem of the need to conduct an energy analysis of such installations was formulated in the works of P. L. Kapitsa.

The more incident energy is transferred to the coolant flowing in the collector, the higher

its efficiency. It can be increased by using special optical coatings that do not emit heat in the infrared spectrum. All existing solar collectors in the world differ mainly in their design, material and manufacturing technology of their absorbers (Avezova, N. R. Avezov, R. R., Rustamov, N.T., Vakhidov, A., Suleymanov, Sh.I., 2013; Ermuratsky, V.V., Postolatiy, V.M., Koptiyuk, E. P., 2009). At the same time, the option of increasing the efficiency of the collector by changing the location of the absorbers on the aperture area of the collector is not considered.

The development of efficient designs of solar collectors and installations for heat supply to the population, as well as the search for ways and new technologies that are economically advantageous for the use of solar heat supply

systems today, is one of the urgent problems of large-scale use of solar energy in the field of municipal thermal power engineering.

The purpose of the work is to increase the efficiency of using solar rays by solar collectors, due to their operation in a cogenerative mode.

The solution method

The Department of Electrical Engineering of the A. Yassavi International Kazakh Turkish University has developed and patented several fundamentally new designs for the location of absorbers on the aperture area and their shape of solar collectors. In order to reduce heat loss and increase the energy efficiency of solar collectors, an optimal design has been developed, where absorbers in the form of fractals are located on the aperture area of a parabolic concentrator according to the principle of the Fibonacci number. Such a solar installation was called fractal solar collectors ФСК (Rustamov, N. T.,

Meirbekov, A. T., Korganbaev, B. N., Patent No. 2639; Rustamov, N. T., Meirbekov, A. T., Kibishev, A. T., invention No. 36213).

The aperture area of such a collector serves as a reflector of the sunlight passing through and past the absorbers. The reflected rays additionally heat the collector pipes arranged in the form of fractals. Thus, the sun's rays are used multiple times. As a result, the efficiency of the ФСК increases compared to a flat solar collector (Rustamov, N. T., Kibirov, A. T., Israilov, F. M., Ernazar, K. E., 2023; Rustamov, Nassim, Kibishov, Adylkhan, Naci Genc, Shokhrukh Babakhan, Ernazar Kamal, 2023).

This type of solar installation is a battery of a parabolic concentrator (similar in shape to a satellite dish), which focuses reflected sunlight from the aperture area onto receivers located at the focal point (the first fractal). In the presented case, the solar installation allows the consumer to receive m of thermal water of various temperatures.

Figure 1. Toroidal absorber: a), the general design of fractal solar collectors b) If the ФСК operates in cogeneration mode, the efficiency of the solar installation will increase even more.

Based on this concept, the department has developed a cogenerative fractal solar collector

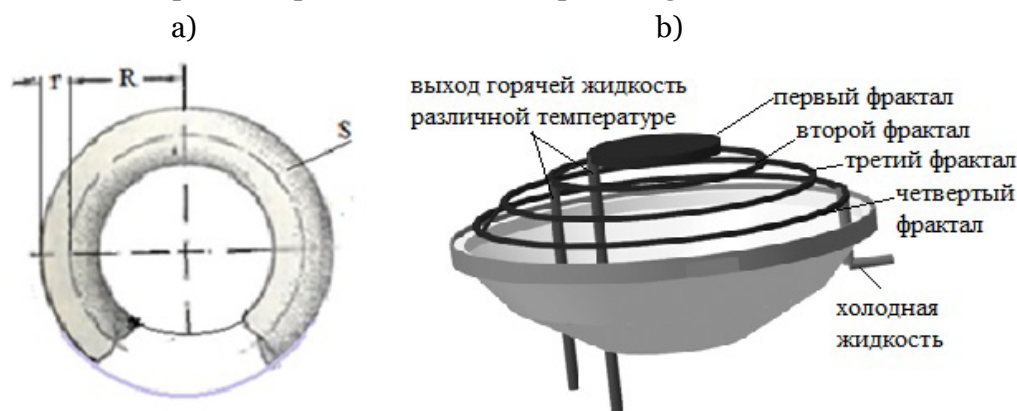
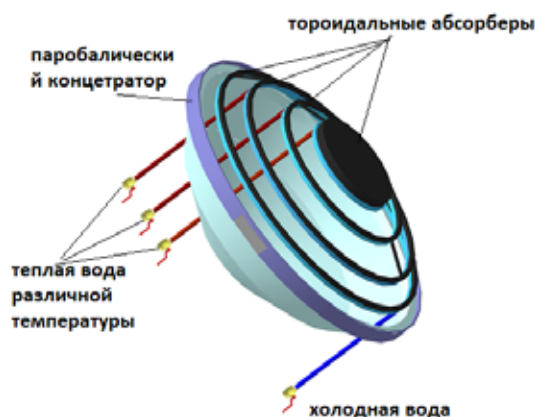


Figure 2. General view of a cogenerative fractal solar collector

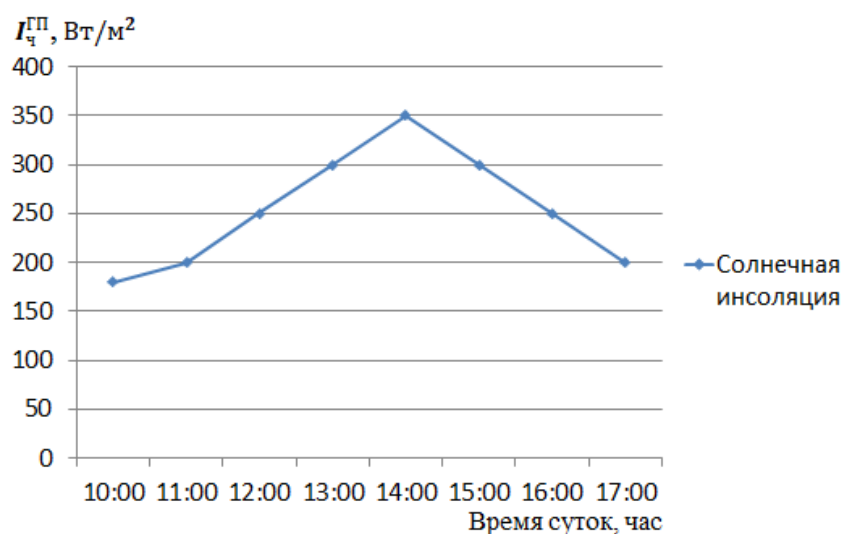


As is known, when a solar installation generates both electrical and thermal energy, then it is said that the solar installation operates in the mode of cogeneration. In order for the ΦCK to work in cogeneration mode, the reverse side of the toroid absorber is sheathed with a polymer photo panel. Then the reflected rays from the aperture area of the collector colliding with the photo panel will generate an electric current. As a result, the ΦCK starts working in cogeneration mode.

During the operation of the $K\Phi CK$, the consumer will receive heat and electricity at the same time, this is the cogeneration of the

solar installation. To assess the thermal and energy characteristics, the $K\Phi CK$ was manufactured according to the method described in (Rustamov, Nassim, Kibishov, Adylkhan, Naci Genc, Shokhrukh Babakhan, Ernazar Kamal, 2023). Based on the experimental data obtained, the ability of the $K\Phi CK$ to absorb solar radiation, the useful power of solar radiation for a solar collector, heat losses, and the electrical power that the solar installation generates were evaluated. All calculations were carried out for solar insolation for the city of Turkestan for the month of March 2023. (Fig. 3).


Figure 3. Daily solar insolation for Turkestan (1.03.2023)




The electrical characteristics of the $K\Phi CK$ were measured every hour. The electric current generated by the solar panels was

measured for each fractal of the $K\Phi CK$. The estimates obtained are shown in Table 1.

Table 1. Energy characteristics in $K\Phi CK$

$K\Phi CK$ Energy description 	Daily hours							
	10⁰⁰	11⁰⁰	12⁰⁰	13⁰⁰	14⁰⁰	15⁰⁰	16⁰⁰	17⁰⁰
$I_4^{ПП}, W / m^2$	180	200	250	300	350	300	250	200
R	2.56	2.18	2.09	2	2	2.09	2.18	2.56
$t_{окр}, ^\circ C$	8	9	10	11	12	13	14	13
$I_4^{ПП}, W / m^2$	460.8	436	522.5	600	700	627	549.4	512
$I_4^{нозл}, W / m^2$	354.8	335.7	402.3	462	539	482.8	423	394.2
$\gamma_4^{mn}, W / m^2$	312	306	300	294	288	282	276	282
$Q_{i_{a1}}^u, W / m^2$	5	8.5	21.9	39.6	60.4	49.5	34.2	24.1

KΦCK Energy description 	Daily hours							
	10 ⁰⁰	11 ⁰⁰	12 ⁰⁰	13 ⁰⁰	14 ⁰⁰	15 ⁰⁰	16 ⁰⁰	17 ⁰⁰
$Q_{l_{a2}}^u, W / m^2$	6.2	10.3	24.7	46.2	78.1	56.9	34.2	26.2
$Q_{l_{a3}}^u, W / m^2$	7.3	12	37.5	50.7	86	66.3	36.1	34.2
$Q_{l_{отр}}^u, W / m^2$	14.7	15.9	17.2	18.4	19.6	21	19.6	17.2
$Q_{обуу}^u, W / m^2$	16.8	18.2	19.6	21	22.4	23.8	22.4	19.6
$\eta_u^{a1}, \%$	21	22.8	24.5	26.3	35	29.8	28	24.5
$\eta_u^{a2}, \%$	52.5	56.9	61.3	65.7	77	74.6	70	61.3
$\eta_u^{a3}, \%$	71	84	145.4	202.2	301.5	247.3	174.5	145.8
$\eta_u^{omp}, \%$	60	70	74	75.4	76	75.3	75	74.6

First of all, we measure the radius of each fractal located in the solar collector, R_1, R_2, R_3 , and the inner radius of the fractal tube r .

$R_1 = 0.15$ m, $R_2 = 0.30$ m, $R_3 = 0.40$ m, $r = 0.016$ m.

Using the measured radii, we calculate the surface area of each fractal pipeline

A_{a1}, A_{a2}, A_{a3} .
 $A_{a1} = 0.13$ m²; $A_{a2} = 0.19$ m²; $A_{a3} = 0.25$ m²;

The hourly values of the useful part of the solar radiation power are found by the formula, $F_R = 0.9$

$$Q_{l_{a1}}^u = A_{F_R} (I_u^{nozл} - \gamma_u^{mn})$$

Where

A – absorber

F_R – is the heat transfer coefficient from the solar collector

$I_u^{nozл}$ – the corresponding hourly values of absorbed solar radiation

γ_u^{mn} – hourly value of heat losses

For the first absorber

$$Q_{l_{a1}}^{12^{00}} = A_{a1} F_R (I_{12^{00}}^{nozл} - \gamma_{12^{00}}^{mn}) = 0.13 * 0.9(704,8 - 300) = 47.4 \text{ W} / \text{m}^2$$

For the second absorber

$$Q_{l_{a2}}^{12^{00}} = A_{a2} F_R (I_{12^{00}}^{nozл} - \gamma_{12^{00}}^{mn}) = 0.19 * 0.9(704,8 - 300) = 69.2 \text{ W} / \text{m}^2$$

For the second absorber

$$Q_{l_{a3}}^{12^{00}} = A_{a3} F_R (I_{12^{00}}^{nozл} - \gamma_{12^{00}}^{mn}) = 0.25 * 0.9(704,8 - 300) = 91.1 \text{ W} / \text{m}^2$$

We determine the area of the solar panel under each absorber A_1, A_2, A_3

We determine the area of the solar panel under the first absorber A_1

R_1 – is the first radius of the fractal (0.15 m)

$$A_1 = \pi R_1^2 = 3.14 * 0.15^2 = 0.07 \text{ m}^2$$

The area of the solar panel under the second absorber is determined by the formula A_2

$$A_2 = l_2 * a$$

First of all, we measure the length of the second fractal $l_2 = 2\pi R_2, R_2 = 0,3$ m

$$l_2 = 2\pi R_2 = 2 * 3.14 * 0,3 = 1.9 \text{ m}$$

Now let's determine the area of the solar panel under the second absorber A_2

$$A_2 = l_2 * a$$

a – the width of the solar panel, $a = 0.04$ m

$$A_2 = l_2 * a = 1.9 * 0.04 = 0.08 \text{ m}^2$$

We determine the area of the solar panel under the third absorber A_3

We measure the length of the third fractal $l_3 = 2\pi R_3$ where $R_3 = 0,4$ m

$$l_3 = 2\pi R_3 = 2 * 3.14 * 0,4 = 2.6 \text{ m}$$

The area of the solar panel under the third absorber is determined by the formula

$$A_3 = l_3 * a$$

$$A_3 = l_3 * a = 2.6 * 0.04 = 0.1 \text{ m}^2$$

The power of the solar panel is determined by the formula P

$$P = A * \eta * I_{\text{луч}} \tag{9}$$

where

A – solar panel area m²

η – the percentage of solar panel efficiency of 15% is 0.15

$I_{\text{луч}}$ – radiance is the radiant power of reflected solar radiation w / m^2

We find the area of the area of reflection of sunlight

$$A_{\text{пар}} = \pi(h^2 + 2a^2) = 3.14 * (0.25^2 + 2 * (0.40)^2) = 1.2 m^2$$

$$A_{\text{абсор}} = A_1 + A_2 + A_3 = 0.13 + 0.19 + 0.25 = 0.57 m^2$$

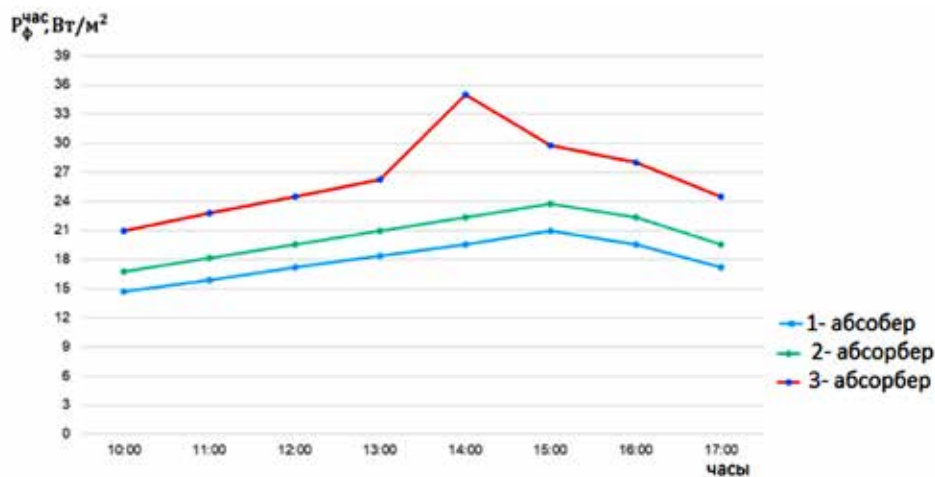
$$A_{\text{кв.плоск}} = A_{\text{пар}} - A_{\text{абсор}} = 1.2 - 0.57 = 0.63 m^2$$

Calculate the value of reflected solar radiation from a parabolic concentrator, $F_R = 0.9$;

$$A_{\text{кв.плоск}} = 0.63 m^2.$$

$$I_{\text{луч}}^{12^{00}} = A_{\text{у.у.}} F_R (I_{12^{00}}^{\text{ж.у.}} - \gamma_{12^{00}}^{\text{ТТ}}) = 0.63 * 0.9(704.8 - 300) = 229.5 W / m^2$$

Figure 4. Graph of the electric power on the solar panel in each fractal of the КФСК by the hour



Doubles the value of solar radiation reflected from a parabolic concentrator

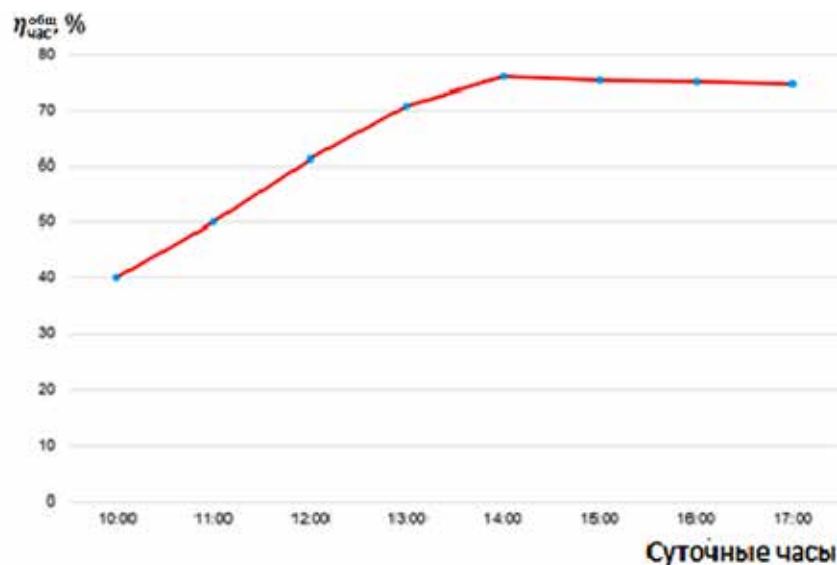
Using formula (9), we find the power of the solar panel on each fractal of the КФСК P_1, P_2, P_3

$$P_1 = A_1 * \eta * I_{\text{луч}}^{12^{00}} = 0.07 * 0.35 * 700 = 17.2 W$$

$$P_2 = A_2 * \eta * I_{\text{луч}}^{12^{00}} = 0.08 * 0.35 * 700 = 19.6 W$$

$$P_3 = A_3 * \eta * I_{\text{луч}}^{12^{00}} = 0.1 * 0.35 * 700 = 24.5 W$$

Figure 5. Dynamics of efficiency by daily hours to КФСК



We calculate the total power received from the solar panel from КФСК at 12:00

$$P_{общ} = P_1 + P_2 + P_3 = 17.2 + 19.6 + 24.5 = 61.3 \text{ W}$$

Analyzing this graph, we can add that the generation of electric energy using a water-heating solar installation has a number of advantages. Our experiments have shown that the generated electric energy by a water-heating solar installation can meet the needs of the solar installation itself. Thus, we can verify the effectiveness of the КФСК. Below we present the dynamics of efficiency changes.

An assessment of such dynamics of a water heating solar installation makes it possible for the consumer to optimize the operating time of this solar installation.

As an example, we will show the dynamics of the efficiency of a cogenerative fractal solar collector in eight hours. To do this, we selected the following initial values from Table 1.

$$I_{12^{00}}^{H\Pi} = 555.5 \frac{\text{Вт}}{\text{м}^2}; Q_{общ}^{12^{00}} = 196.5 \frac{\text{Вт}}{\text{м}^2};$$

$$P_{общ}^{12^{00}} = 17.25 \text{ W};$$

The efficiency for the CFSC as a whole, where we determined the total area of the solar panel $A_{\text{кв.плоск}} = 0.63 \text{ м}^2$

$$\eta_{12^{00}}^{общ} = \frac{Q_{общ}^{12^{00}} + P_{общ}^{12^{00}}}{A_{общ} I_{12^{00}}^{H\Pi}} * 100 =$$

$$= \frac{196.5 + 61.3}{0.63 * 555.5} * 100 = 74\%$$

Taking into account the corresponding hourly electrical values of the КФСК $Q_{общ}^u$ and $I_u^{H\Pi}$, their daily (total) values are determined by the formulas $Q \Sigma Q_{общ}^u$ и $\Sigma I_u^{H\Pi}$, using formula (9), we found the daily efficiency of CFSC:

$$\eta_{\text{КФСК}_{\text{сут}}} = \frac{\Sigma Q_{общ}^u}{A_{\text{абсор}} \Sigma I_u^{H\Pi}} * 100 =$$

$$= \frac{71 + 84 + 145.4 + 202.2 + 301.5 + 247.3 + 174.5 + 145.8}{0.63 * (460.8 + 436 + 522.5 + 600 + 700 + 627 + 549.4 + 512)} * 100 =$$

$$= \frac{1371.7}{4407.7 * 0.48} * 100 = 71.3\%$$

Using the following empirical formula in the КФСК, we determined the average daily value of efficiency:

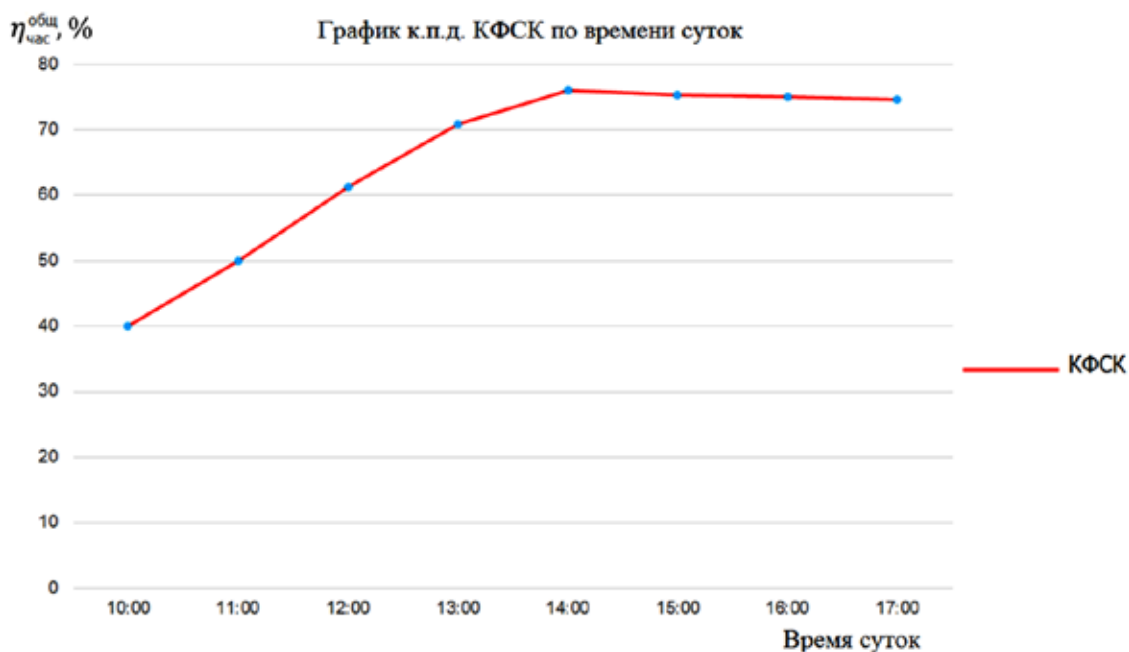
$$\eta_{\text{КФСК}_{\text{сут}}}^{\text{сред}} = \frac{\Sigma \eta_{общ}}{n} =$$

$$= \frac{71 + 84 + 145.4 + 202.2 + 301.5 + 247.3 + 174.5 + 145.8}{24} =$$

$$= 58.3\%$$

where $\eta_{общ} = \Sigma \eta_{час}$ – the hourly efficiency values in the КФСК are taken from Formula (7).

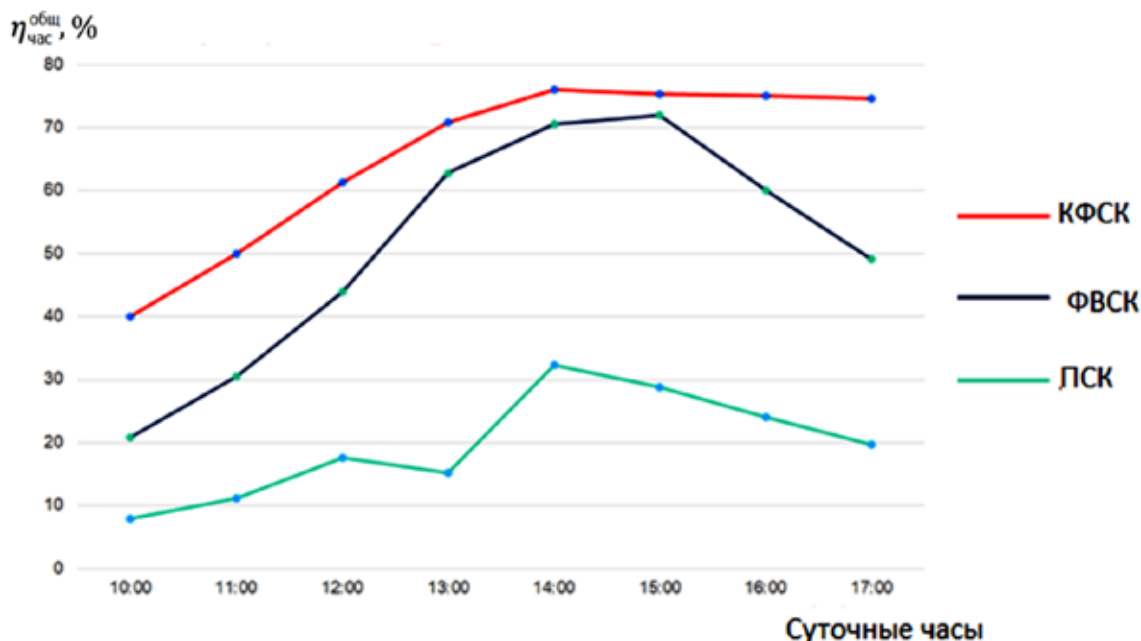
Figure 6. Dynamics of changes in the efficiency of a cogenerative fractal solar collector



Now let's consider a retrospective analysis of the efficiency of three solar collectors ПСК, ФВСК and КФСК. The efficiency data for a fractal evacuated collector (ФВСК) and

a flat solar collector (ПСК) are taken from (Rustamov, Nassim, Kibishov, Adylkhan, Naci Genc, Shokhrukh Babakhan, Ernazar Kamal, 2023).

Figure 7. Retrospective analysis of the efficiency of three solar installations



This graph confirms the concept that was given at the beginning of the article. The positive and negative results obtained during the experiments stimulate the further development of research in this direction.

Conclusions

The use of solar collectors due to solar energy can reduce the cost of heating and hot water. Recent studies have shown that by changing the design of the absorbers in the aperture area, the use of solar insolation in a solar installation can increase its efficiency. The efficiency of installations performed with

such a design can reach 80–85%. The new type of solar collector described in this paper is called a cogenerative fractal solar collector (КФСК). On the other hand, the creation of a КФСК producing both heat and electricity will stimulate the further development of solar collectors.

According to the results of the experiment, it can be said that the КФСК has shown itself to be on the good side in terms of the simplicity of its design and the low cost of consumable material, small footprint, and the efficiency of using solar insolation.

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